

# NUCLEI

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Nucleus  $\rightarrow$  Atomic nucleus is made up of +vely charged protons and neutron neutrons.

$$m_p = 1.6726 \times 10^{-27} \text{ kg} = 1835 m_e$$

$$\text{and } m_n = 1.6749 \times 10^{-27} \text{ kg} = 1839 m_e$$

$m_p$  is almost equal to  $m_n$ .

① Nucleons  $\rightarrow$  Protons and neutrons present in the nucleus of an atom are called nucleons.

② Atomic number  $\rightarrow$  The number of protons present in the nucleus of an atom is called atomic number of the nucleus element.

In a  ${}_Z^X$  nucleus of X element

$$Z = \text{no. of protons} = \text{no. of electrons in a neutral atom} \\ = \text{Atomic number of the X element.}$$

e.g. in  ${}_6^{12}\text{C}$ , 6 is the atomic number of carbon.

③ Mass number  $\rightarrow$  The total number of nucleons present in the nucleus of an atom is called mass number of the element.

In  ${}_Z^X$  nucleus of X element

$$A = \text{no. of nucleon} = \text{no. of protons} + \text{no. of neutrons} \\ = \text{Mass number of X element.}$$

$$\therefore A - Z = \text{no. of neutrons}$$

e.g. in  ${}_{17}\text{Cl}^{35}$ , 35 is the mass number the  $\text{Cl}$  and  $35 - 17 = 18 = \text{no. of neutrons}$ .

4. Also in gold nucleus represented by  ${}_{79}\text{Au}^{197}$   
no. of protons = 79

$\therefore$  ~~mass~~ Atomic number = 79.

No. of nucleons = 197

$\therefore$  Mass number = 197

and no. of neutrons =  $A - Z = 197 - 79 = 118$ .

### Isotopes $\rightarrow$

The atom of an element which have same atomic number but different mass numbers are called isotopes.

They exhibit almost same chemical properties

e.g. isotopes of hydrogen are  ${}_{1}\text{H}^1$  (protium)

${}_{1}\text{H}^2$  (deuterium)

${}_{1}\text{H}^3$  (tritium)

and isotopes of carbon are  ${}_{6}\text{C}^{11}$ ,  ${}_{6}\text{C}^{12}$ ,  ${}_{6}\text{C}^{13}$ ,  ${}_{6}\text{C}^{14}$ .

### Isobars $\rightarrow$

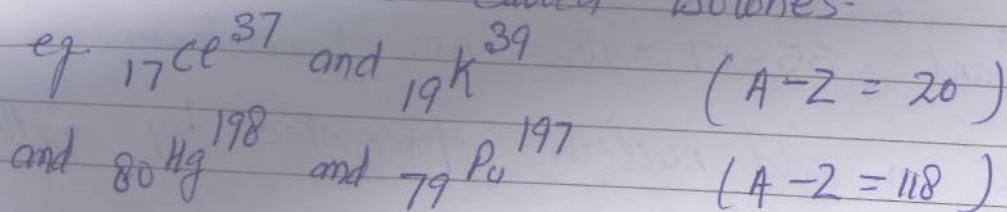
The atoms of the different elements which have different atomic numbers but same mass number are called isobars.

Since these elements contain different no. of electrons therefore they exhibit diff. chemical properties

eg  ${}_{11}\text{B}^3$  and  ${}_{2}\text{He}^3$   
 ${}_{17}\text{Cl}^{37}$  and  ${}_{16}\text{S}^{37}$

or  ${}_{20}\text{Ca}^{40}$  and  ${}_{18}\text{Ar}^{40}$ .

**Isotones**  $\rightarrow$  The nuclides having same number of neutrons are called isotones.



**Isomers**  $\rightarrow$

These are the nuclei with same atomic number and same <sup>mass</sup> number but existing in different energy states.

eg. a nucleus in ground state and same nucleus in metastable excited state are isomers.

eg.  ${}_{28}\text{Ni}^{60}$  in ground state and  ${}_{28}\text{Ni}^{60}$  in excited state are isomers.

**Atomic mass unit**  $\rightarrow$  One amu is d/a the  $\frac{1}{12}$ th of mass of  ${}_{6}\text{C}^{12}$  atom.

$$\text{i.e. } 1 \text{ amu} = \frac{1}{12} \times \text{mass of } {}_{6}\text{C}^{12} \text{ atom}$$

$$\therefore 1 \text{ amu} = 1.66 \times 10^{-27} \text{ kg}$$

This unit is used to measure the masses of atomic particles.

$$m_p = 1.6726 \times 10^{-27} \text{ kg} = 1.0073 \text{ amu}$$

$$m_n = 1.6749 \times 10^{-27} \text{ kg} = 1.0086 \text{ amu}$$

$$m_H = 1.0078 \text{ amu} \quad (\because m_p + m_e = m_H)$$

**Electron volt**  $\rightarrow$  Energy possessed by an electron, when it is accelerated by applying a potential difference of one volt is called 1 electron volt (or 1 eV)

$$\begin{aligned} \text{i.e. } 1 \text{ eV} &= 1e \times 1V \\ &= 1.6 \times 10^{-19} \text{ C} \times 1V \\ &= 1.6 \times 10^{-19} \text{ CV} \end{aligned}$$

$$\Rightarrow \boxed{1 \text{ eV} = 1.6 \times 10^{-19} \text{ J}}$$

$$\text{and } 1 \text{ MeV} = 1.6 \times 10^{-13} \text{ J.}$$

**Relation b/w amu and MeV**  $\rightarrow$  According to Einstein's mass energy relationship

$$E = mc^2$$

i.e.  $m$  unit of mass can produce  $E$  unit of energy

$$\text{if } m = 1 \text{ amu} = 1.66 \times 10^{-27} \text{ kg.}$$

$$\text{then } E = 1.66 \times 10^{-27} \text{ kg} \times (3 \times 10^8 \text{ ms}^{-1})^2$$

$$= 1.66 \times 10^{-27} \times 9 \times 10^{16} \text{ kg m}^2 \text{ s}^{-2}$$

$$= 14.94 \times 10^{-11} \text{ J}$$

$$= \frac{14.94 \times 10^{-11}}{1.6 \times 10^{-13}} \text{ MeV}$$

$$E = 931 \text{ MeV.}$$

i.e. 1 amu of mass can produce 931 MeV of energy

**Nuclear size**  $\rightarrow$  Surface of nucleus is not a well defined boundaries. However Rutherford scattering experiment helps us to estimate the size of the nucleus.

It was found out experimentally that volume of the nucleus is directly proportional to its mass number

$$\text{i.e. } \frac{4}{3} \pi R^3 \propto A$$

$$\Rightarrow R^3 \propto A$$

$$\Rightarrow R \propto A^{1/3}$$

$$\Rightarrow R = R_0 A^{1/3}$$

where  $R_0 = 1.2 \times 10^{-15} \text{ m} = 1.2 \text{ fm} = \text{const.}$

Thus radius of the nucleus is directly proportional to cube root of mass number.

**Nuclear density**  $\rightarrow$  we know that Let  $m$  is the avg. mass of the nucleon of  $Z^A$  nucleus of radius  $R$ .

Thus Density of nucleus =  $\frac{\text{Mass of the nucleus}}{\text{Volume of the nucleus}}$

$$\text{i.e. } \rho = \frac{mA}{\frac{4}{3} \pi R^3}$$

$$= \frac{mA}{\frac{4}{3}\pi(R_0 A^{1/3})^3}$$

$$= \frac{mA}{\frac{4}{3}\pi R_0^3 A}$$

$$\Rightarrow \rho = \frac{3m}{4\pi R_0^3} = \text{Const.}$$

i.e.  $\rho$  density of nucleus is independent of the mass number of the nucleus. i.e. density of hydrogen nucleus and density of iron nucleus is same.

i.e. Two identical boxes one containing hydrogen nuclei and other containing iron nuclei will have same mass.

On substituting the standard values

$$\rho = 2.3 \times 10^{17} \text{ Kg m}^{-3}$$

(Very high in comparison to density of water i.e.  $1.0 \times 10^3 \text{ Kg m}^{-3}$ )

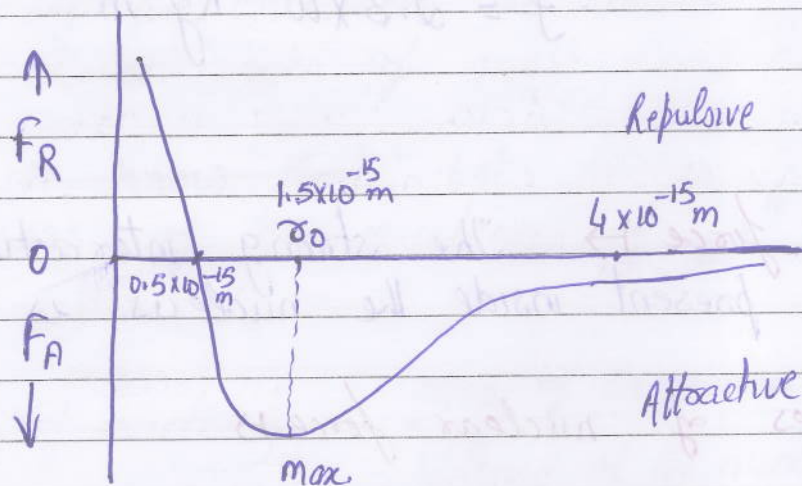
**Nuclear force**  $\Rightarrow$  The strong interaction b/w the nucleons present inside the nucleus is called nuclear force

**properties of nuclear force**  $\Rightarrow$

① It is strongest force in nature. This force binds the nucleons together in the nucleus despite of the electrostatic force of repulsion b/w the protons

$$F_N : F_{ES} : F_{\text{weak}} : F_G = 10^{38} : 10^{36} : 10^{25} : 1$$

- ② Nuclear forces are short range forces. i.e. these forces act only if the distance b/w nucleon is very-very small.
3. Nuclear forces are independent of the charge on the nucleon i.e. nuclear force b/w p. and p, n and n or n and p is same provided the distance b/w them is same.
4. Cause of these forces is exchange of elementary particle  $\pi$ -meson b/w the nucleons.
5. Nuclear forces are non central force i.e. it does not act along the line joining the centres of two nucleons.
6. Nuclear force varies with distance b/w the nucleon as shown in the graph.



for a distance more than  $4 \times 10^{-15} \text{ m} = 4 \text{ fm}$  nuclear force is almost zero (i.e. short range force)

## Mass Defect and packing fraction $\rightarrow$

It is found that mass of the stable nucleus is always less than the sum of the mass of its constituent nucleons.

The difference b/w the sum of rest mass of the nucleons present in the nucleus and actual mass of nucleus is called mass defect.

It is denoted by  $\Delta m$ .

Consider a  ${}_Z^A$  nucleus having mass  $M_N$  and  $Z$  protons each of mass  $m_p$  and  $(A-Z)$  neutrons each of mass  $m_n$  then mass defect is

$$\Delta m = Z m_p + (A-Z) m_n - M_N$$

$$\text{or } \Delta m = Z m_p + Z m_e + (A-Z) m_n - M_N - Z m_e$$

(where  $m_p + m_e = m_H$  and  $M_N + Z m_e = M_X = \text{mass of } X$ )

Packing fraction  $\rightarrow$  Mass defect per nucleon of the nucleus is called its packing fraction.

$0 \rightarrow \sim +ve$  i.e. Packing fraction of nucleus =  $\frac{\Delta m}{A}$ .

$0 +ve \rightarrow \sim$  for nuclei having mass number  $< 20$  and  $> 200$ , packing fraction (or mass defect is ~~is~~ ve) and such nuclei are unstable nuclei.

while for nuclei having mass number  $> 20$  and  $< 200$ , packing fraction (or mass defect) is +ve and such nuclei are stable nuclei.

## Binding Energy and Binding energy per nucleon $\rightarrow$

To form a nucleus i.e. bringing the nucleons together in the nucleus, some work has to be done against the electrostatic force of repulsion.



This energy required to bind all the nucleons together in the nucleus is called binding energy.

On the contrary, similar amount of energy is required to break up the nucleus into its constituent nucleons and place them at infinite distance from each other, so that they may not interact with each other.

Thus binding energy may also be defined as the energy required to split up the nucleus into its constituent nucleon and separate them to such a large distance so that they may not interact with each other.

We know that for a stable nucleus sum of the masses of ~~nucleus~~ nucleons is always more than mass of stable nucleus. It is because some part of the mass of the nucleons get converted into binding energy which holds the nucleons together in the nucleus.

from Einstein's mass energy relationship.

$$B.E = \text{mass defect} \times c^2$$

$$\text{i.e. } \boxed{B.E = \Delta m c^2}$$

$$\boxed{B.E = [Zm_p + (A-Z)m_n - M_N] c^2}$$

or.  $B.E = [Zm_p + Zm_e + (A-Z)m_n - M_N - Zm_e] c^2$

$$\Rightarrow B.E = [Z(m_p + m_e) + (A-Z)m_n - (M_N + Zm_e)]c^2$$

$$\Rightarrow B.E = [ZM_H + (A-Z)m_n - M_x]c^2$$

where  $M_H = m_p + m_e =$  mass of hydrogen atom

and  $M_x = M_N + Zm_e =$  mass of  $x$  atom.

**Binding energy per nucleon**  $\rightarrow$  The energy required to remove first nucleon from the nucleus is not same as that of removing 2nd or 3rd or

Thus avg. energy required to extract one nucleon from the nucleus is called binding energy per nucleon.

Mathematically,

$$B.E. \text{ per nucleon} = \frac{B.E}{\text{number of nucleon}}$$

$$= \frac{[ZM_H + (A-Z)m_n - M_x]c^2}{A}$$

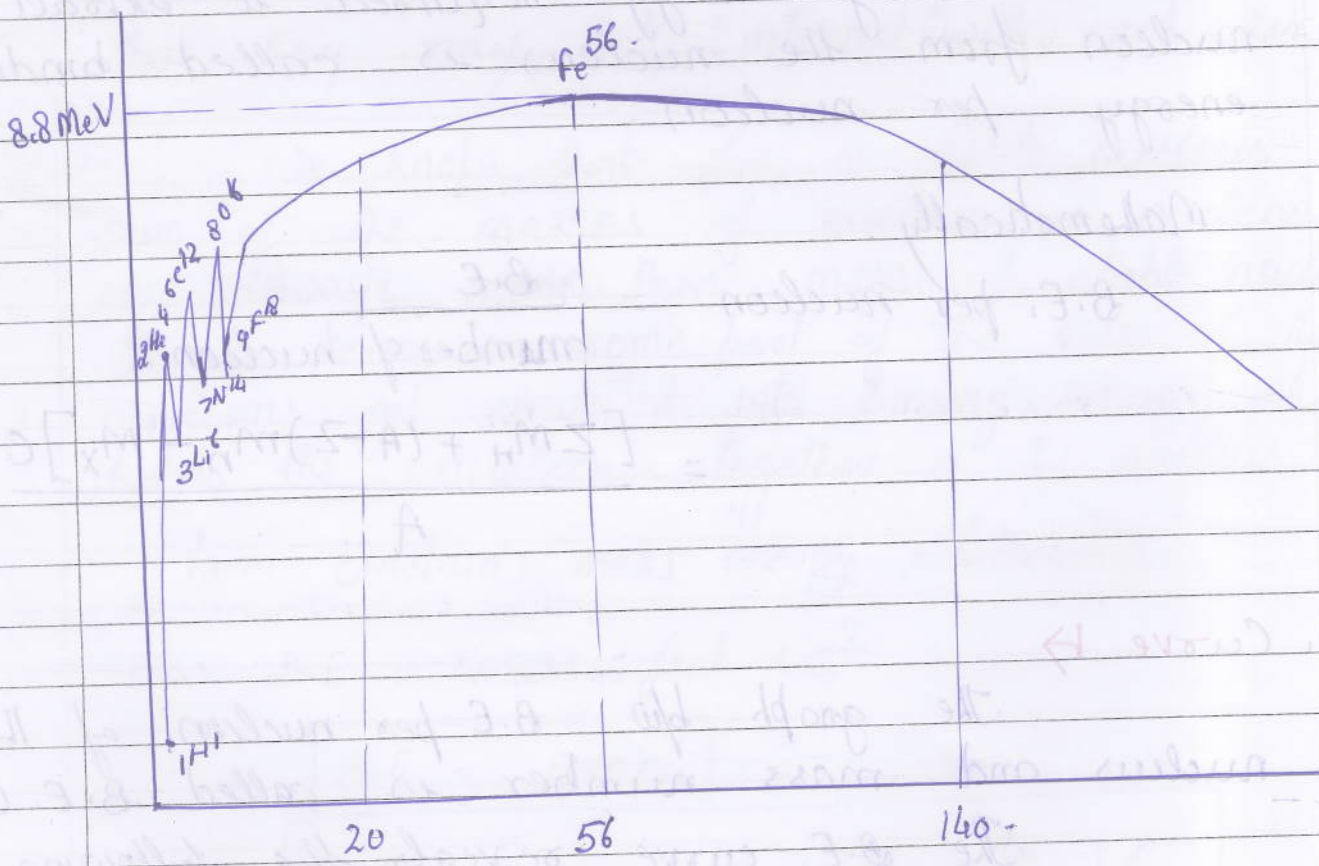
**B.E. Curve**  $\rightarrow$

The graph b/w B.E per nucleon of the nucleus and mass number is called B.E. Curve.

The B.E. curve reveals the following facts

- ① The B.E./nucleon for smaller or light nuclei is small. i.e. light nuclei are comparatively less stable.

2. We get certain peaks in the B.E curve for  ${}^2\text{He}_4$ ,  ${}^6\text{C}_{12}$ ,  ${}^{16}\text{O}_8$ . It shows that these nuclei are comparatively more stable than their neighbouring nuclei.
3. B.E. curve is almost flat for mass numbers b/w 20 to 140. However B.E per nucleon for  $\text{Fe}^{56}$  is maximum (8.8 MeV). Thus we can say that iron is most stable element.
4. B.E./nucleon ~~decto~~ decreases gradually for mass numbers above 140. Thus these nuclei are again unstable and emit elementary particles.



Ques H How B.E curve can be used to explain the phenomena of nuclear fission or fusion.

Ans  $\rightarrow$  From the B.E curve it is clear that B.E per nucleon of the heavier nuclei like  $U^{235}$  is very small as compared to B.E per nucleon for  $Ba^{141}$  or  $Kr^{92}$ . Thus in order to attain more stability  $U^{235}$  splits up into  $Ba^{141}$  and  $Kr^{92}$ .

Similarly B.E per nucleon of  ${}^1_1H$  is very small as compared to that of  ${}^4_2He$ . Thus in order to attain more B.E and hence more stability,  ${}^1_1H$  nuclei fuse together to give  ${}^4_2He$  nucleus.

Ques  $\rightarrow$  Calculate the mass defect, P.F, B.E and B.E per nucleon of  ${}_{20}Ca^{40}$ .

Given  $m_p = \cancel{1.008665} 1.007825$  amu.

$m_n = 1.008665$  amu.

and  $M_{Ca} = 39.962589$  amu.

Ans  $\rightarrow$  We know that  ${}_{20}Ca^{40}$  contains 20 protons and 20 neutrons.

$$\begin{aligned} \therefore \text{Sum of masses of nucleons} &= Z m_p + (A-Z) m_n \\ &= 20 \times 1.007825 + 20 \times 1.008665 \\ &= 20.1565 + 20.1733 \\ &= 40.3298 \text{ amu.} \end{aligned}$$

Actual mass of  ${}_{20}Ca^{40}$  nucleus,  $M_{Ca} = 39.962589$  amu.

Thus mass defect  $\Delta m = 40.3298 - 39.962589$   
 $= 0.367211$  amu.

$\therefore$  Packing fraction  $= \frac{\Delta m}{A} = \frac{0.367211}{40} = 0.009180275$  amu

$$\therefore B.E = \left( \frac{\Delta m}{1 \text{ amu}} \right) \times 931 \text{ MeV}$$

$$= 0.367211 \times 931 \text{ MeV}$$

$$= 341.87 \text{ MeV}$$

$\therefore 1 \text{ amu}$  produces  
931 MeV of energy

$$\therefore B.E \text{ per nucleon} = \frac{341.87}{40} \text{ MeV}$$

$$= 8.547 \text{ MeV}$$

$$Q = BE_P - BE_R$$

$$Q = (M_R - M_P) c^2 \times 931$$

Sum of masses of reactants =  $5 m_p + (4-5) m_n$

$$= 5 \times 1.007825 + 4 \times 1.008665 = 9.0313175 \text{ amu}$$

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$$= 5 \times 1.007825 + 4 \times 1.008665 = 9.0313175 \text{ amu}$$

Actual mass of  ${}^4_2\text{He}$  nucleus,  $M_P = 4.002603 \text{ amu}$

Thus mass defect  $\Delta m = 9.0313175 - 4.002603 = 5.0287145 \text{ amu}$

$$= 5.0287145 \text{ amu}$$

$$B.E = \Delta m \times 931 = 5.0287145 \times 931 = 4681.75 \text{ MeV}$$