

UNIT - 1 ELECTRO STATICS

(Marks - 8)

DATE

Frictional Electricity :->

Electrostatics is the study of electric charges at rest.

When ever two bodies are rubbed with each other, heat energy is produced due to force of friction b/w the two bodies. Due to this heat electrons get transferred from one body (having lower value of Ionization Energy) to the other body having higher value of I.E. Thus both the bodies acquire charges. Thus electrostatics is also named frictional electricity or static electricity.

Two Kinds of Charges :->

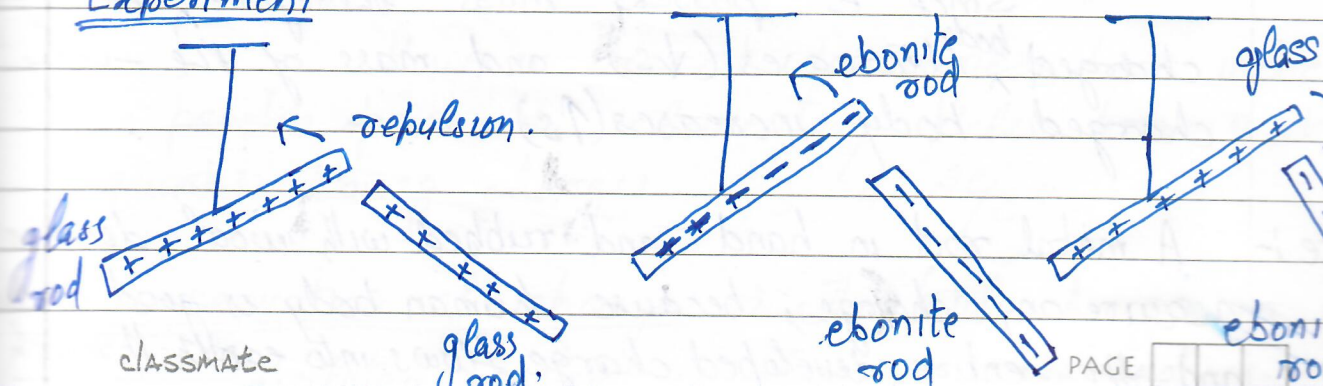
When two bodies are rubbed with each other, transfer of e^- s takes place. A body which loses e^- s acquires +ve charge w/a the body which gains charge e^- acquires -ve charge.

eg. when glass rod is rubbed with silk cloth, then glass rod acquires +ve charge w/a silk cloth acquires -ve charge.

Similarly when ebonite rod is rubbed with fur then ebonite rod acquires -ve charge and fur acquires +ve charge.

Like charges repel each other w/a unlike charges attract each other.

Experiment



When a glass rod rubbed with silk cloth is brought near another freely suspended glass rod rubbed with silk then both rods repel each other.

||ly when a ebonite rod (or plastic rod) rubbed with fur (or silk) is brought near to a such ebonite rod then again both the rods repel each other.

But when a ebonite rod rubbed with fur is brought near a freely suspended glass rod rubbed with silk then both rods attract each other.

Thus we can say that like charge repel and unlike charges attract each other. This statement is also k/a fundamental law of electrostatics.

Cause of electrostatics \rightarrow

When two bodies are rubbed with each other then due to force of friction, heat energy is produced. Thus e^- s get transferred from a body having lower work function (or lower I.E) to the body having higher work function (or higher I.E). The body which loses e^- s acquire +ve charge and is k/a vicious body and where as the body which gains e^- s acquire -ve charge and is k/a resonant body.

Since e^- s possess mass therefore, the ^{mass of} +ve charged ^{body} decreases (\downarrow s) and mass of the -vely charged body increases (\uparrow s).

Note:- A metal rod in hand and rubbed with wool does not acquire any charge, because human body is good conductor and the entire developed charge flows into earth through the ground.

Basic properties of electric charges \rightarrow

- 1) Charge on any body does not varies with velocity as mass varies as per:-

$$m = \frac{m_0}{\sqrt{1 - \frac{u^2}{c^2}}}$$

- 2) Charges are additive in nature i.e. they can be added algebraically.

eg $\boxed{+2C + 3C} = +5C$ $\boxed{+2C - 3C} = -1C$.

- 3) Charge is quantized in nature. i.e. any body possess charge equals to integral multiple of charge on one e^- i.e.

$$\boxed{q = \pm ne}$$
 where n is any integer
and $e = -1.6 \times 10^{-19} \text{ C}$.

Cause of quantization of charge is that the charge of any body is due to transfer of integral number of e^- 's from one body to another body.

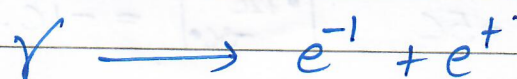
eg when 10 e^- 's will transfer from one body to other then one body will acquire $+10e$ charge and other will acquire $-10e$ charge. And it is never possible that $10\frac{1}{2} e^-$ get transferred.

However recent discoveries have indicated the ~~particles~~ elementary particles known as quarks having charges $e/3$ & $2e/3$.

- 4) Conservation of charges \rightarrow The total charge on a classmate isolated system is always conserved. PAGE

eg. (a) when a glass rod is rubbed with silk cloth then glass rod acquires +ve charge w/ silk cloth acquires equal -ve charge. Therefore total charge before and after rubbing remain same (here zero)

(b) In pair production, a γ ray photon breaks up to produce an electron and positron. Thus total charge before and after pair production remains same.



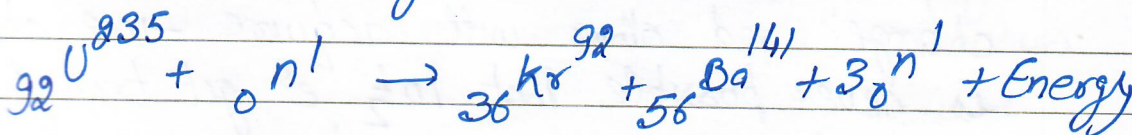
charge 0 (neutral) \longrightarrow $-1e + 1e$ (0)

(c) In ~~annihilation~~ annihilation of matter, an electron and positron destroy each other to produce γ ray photon.



charge (0) \longrightarrow (0)

(d) In all types of nuclear transformation the total charge before and after transformation remains same. eg.



Charge $92 + 0 \longrightarrow 36 + 56 + 0$.

ee $92 \longrightarrow 92$.

Coulomb's Law of Electric Forces \rightarrow

According to Coulomb's law, the force of attraction or repulsion b/w two charges is directly proportional to the product of charges and inversely proportional to the square of distance b/w them.

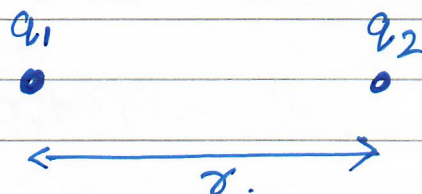
Consider two charges q_1 & q_2 separated in vacuum by a distance r then force of attraction or repulsion b/w them is

$$F \propto q_1 q_2$$

$$\propto \frac{1}{r^2}$$

$$\Rightarrow F \propto \frac{q_1 q_2}{r^2}$$

$$\Rightarrow F = k \frac{q_1 q_2}{r^2}$$



where $k = \frac{1}{4\pi\epsilon_0}$ is constant of proportionality, and ϵ_0 is electrical permittivity of the vacuum free space.

$$\therefore F = \frac{1}{4\pi\epsilon_0} \frac{q_1 q_2}{r^2}$$

where $\frac{1}{4\pi\epsilon_0} = 9 \times 10^9 \text{ N m}^2 \text{ C}^{-2}$

Units of Charge \rightarrow

we know that (wkt)

$$F = \frac{1}{4\pi\epsilon_0} \frac{q_1 q_2}{r^2}$$

if $q_1 = q_2 = 1\text{C}$ and $r = 1\text{m}$

then $F = 9 \times 10^9 \text{ N m}^2 \text{ C}^{-2} \times \frac{1\text{C} \times 1\text{C}}{1\text{m}^2}$

classmate $\Rightarrow F = 9 \times 10^9 \text{ N}$

Thus charge is said to be IC if it attracts or repels an equal charge placed at a distance of 1m in vacuum with a force of 9×10^9 N.

In cgs system, the unit of charge is one statcoulomb or electrostatic unit of charge and ~~1 esu of charge or 1 statcoulomb = 3×10^9 e~~

1 Coulomb = 3×10^9 statcoulomb ~~or (statcoulomb)~~

and electromagnetic unit of charge as abcoulomb

and 1 Coulomb = $\frac{1}{10}$ emu of charge = $\frac{1}{10}$ abcoulomb

~~Color~~

Coulomb's law in vector form: \rightarrow

Consider two charges q_1 and q_2 so that $q_1 \times q_2 > 0$ separated by a distance r as shown. Let F_{12} is the force exerted by q_2 on q_1 and F_{21} " " " " " " q_1 on q_2

Then from Coulomb's law:-

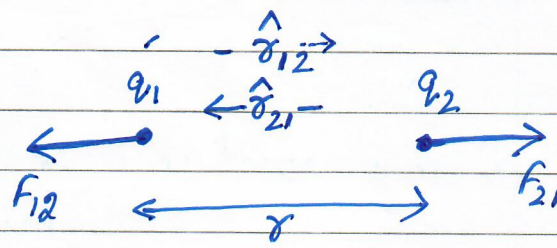
$$\vec{F}_{12} = \frac{1}{4\pi\epsilon_0} \frac{q_1 q_2}{r^2} \hat{\sigma}_{21}$$
 ①

~~||ly $\vec{F}_{21} = \frac{1}{4\pi\epsilon_0} \frac{q_1 q_2}{r^2} \hat{\sigma}_{12}$~~

||ly
$$\vec{F}_{21} = \frac{1}{4\pi\epsilon_0} \frac{q_1 q_2}{r^2} \hat{\sigma}_{12}$$
 ②

But $\hat{\sigma}_{12} = -\hat{\sigma}_{21}$

Thus eqn no ② becomes

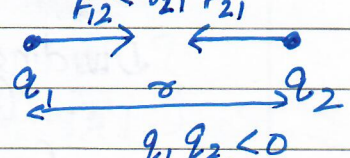


$$\vec{F}_{21} = \frac{1}{4\pi\epsilon_0} \frac{q_1 q_2}{r^2} (-\hat{r}_{21})$$

$$\Rightarrow \vec{F}_{21} = - \frac{1}{4\pi\epsilon_0} \frac{q_1 q_2}{r^2} \hat{r}_{21}$$

$$\Rightarrow \boxed{\vec{F}_{21} = -\vec{F}_{12}} \quad \text{from } \{ \text{using eqn ①} \}$$

Thus force exerted by two charges on each other is equal and opposite.

if $q_1 q_2 < 0$ i.e. $q_1 q_2 = -ve$ $-\hat{r}_{12}$
 even then $\vec{F}_{21} = -\vec{F}_{12}$ 

but the force will be attractive in nature

note: $\rightarrow q_1 q_2 > 0 \Rightarrow q_1 q_2 = +ve$ i.e. either both charges are +ve or both are -ve.

$q_1 q_2 < 0 \Rightarrow q_1 q_2 = -ve$ i.e. charges are opposite in nature.

note: \rightarrow Since coulomb's force act along the line joining the centre of two charges therefore it is also called central force.

Dielectric constant (K) or relative permittivity (ϵ_r) \rightarrow
 Dielectric constant or relative permittivity of a medium is defined as (d/a) the ratio of permittivity of the medium to the permittivity of the free space.

$$\text{i.e. } \boxed{K \text{ or } \epsilon_r = \frac{\epsilon}{\epsilon_0}}$$

$$\text{or } \epsilon = K\epsilon_0$$

Consider two charges q_1 and q_2 separated by a distance r in free space. The force b/w them is given as

$$F_0 = \frac{1}{4\pi\epsilon_0} \frac{q_1 q_2}{r^2} \quad \text{--- (1)}$$

q_1
 \bullet

q_2
 \bullet

$\longleftrightarrow r \longrightarrow$

if these two charges are separated by the same distance in med. then

$$F_{med} \text{ or } F_m = \frac{1}{4\pi\epsilon} \frac{q_1 q_2}{r^2} \quad \text{--- (2)}$$

Dividing (1) by (2) we get

$$\frac{F_0}{F_m} = \frac{1}{4\pi\epsilon_0} \frac{q_1 q_2}{r^2} \times \frac{4\pi\epsilon}{1} \times \frac{r^2}{q_1 q_2}$$

$$\Rightarrow \frac{F_0}{F_m} = \frac{\epsilon}{\epsilon_0} = K \text{ or } \epsilon_r$$

thus
 $\epsilon_r \text{ or } K = \frac{F_0}{F_m}$

Thus dielectric constant or relative permittivity may also be d/fo the ratio of force of attraction or repulsion b/w the two charges separated by certain distance in free space to the force of attraction or repulsion b/w the same two charges separated by the same distance in medium.

since $K = \frac{F_0}{F_m}$ or $\epsilon_r = \frac{F_0}{F_m}$

$$\therefore F_m = \frac{F_0}{K} \quad \Rightarrow F_m = \frac{F_0}{\epsilon_r}$$

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$$\Rightarrow F_m = \frac{1}{4\pi\epsilon} \frac{q_1 q_2}{r^2} \quad \Rightarrow F_m = \frac{1}{4\pi\epsilon_0 \epsilon_r} \frac{q_1 q_2}{r^2}$$

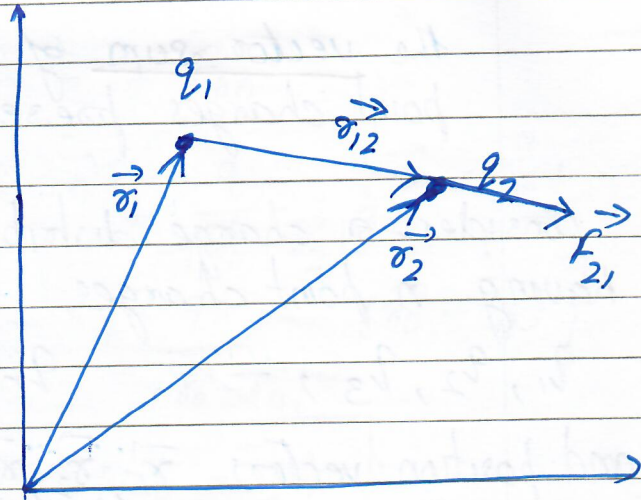
Coulombs law in position vector form \rightarrow

$q_1 q_2 > 0$

Consider two charges q_1 & q_2 having position vectors (PVE) \vec{r}_1 & \vec{r}_2 respectively.

Thus from Coulombs law the force exerted by q_1 on q_2 is

$$\vec{F}_{21} = \frac{1}{4\pi\epsilon_0} \frac{q_1 q_2}{|\vec{r}_{12}|^2} \hat{r}_{12}$$



$$\Rightarrow \vec{F}_{21} = \frac{1}{4\pi\epsilon_0} \frac{q_1 q_2}{|\vec{r}_{12}|^2} \times \frac{\vec{r}_{12}}{|\vec{r}_{12}|} \quad \left\{ \because \hat{A} = \frac{\vec{A}}{|\vec{A}|} \right\}$$

$$\Rightarrow \vec{F}_{21} = \frac{1}{4\pi\epsilon_0} \frac{q_1 q_2}{|\vec{r}_{12}|^3} \vec{r}_{12} \quad \text{--- (1)}$$

From a law of vector addition.

$$\vec{r}_2 = \vec{r}_1 + \vec{r}_{12}$$

$$\Rightarrow \vec{r}_{12} = \vec{r}_2 - \vec{r}_1$$

Thus eqn (1) becomes.

$$\vec{F}_{21} = \frac{1}{4\pi\epsilon_0} \frac{q_1 q_2}{|\vec{r}_2 - \vec{r}_1|^3} (\vec{r}_2 - \vec{r}_1) \quad \text{--- (2)}$$

Similarly force exerted by q_2 on q_1 is

$$\vec{F}_{12} = \frac{1}{4\pi\epsilon_0} \frac{q_1 q_2}{|\vec{r}_{21}|^2} \hat{r}_{21}$$

$$\therefore \text{Similarly } \vec{F}_{12} = \frac{1}{4\pi\epsilon_0} \frac{q_1 q_2}{|\vec{r}_1 - \vec{r}_2|^3} (\vec{r}_1 - \vec{r}_2) \quad \text{--- (3)}$$

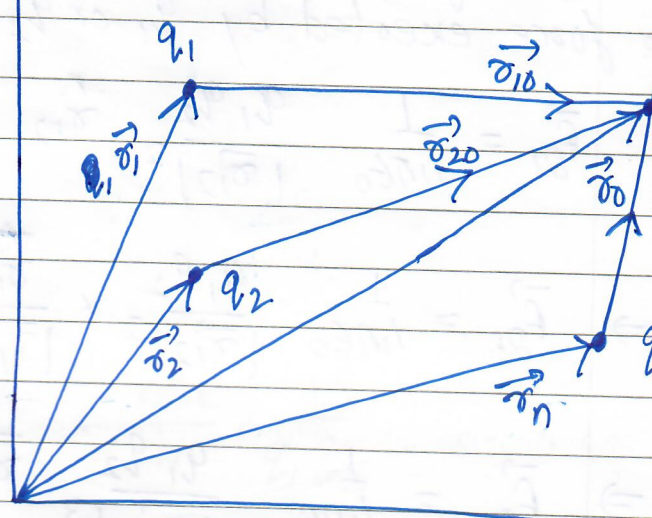
from (2) & (3)

$$\vec{F}_{12} = -\vec{F}_{21}$$

Superposition principle \rightarrow According to superposition principle the net force on a given charge is the vector sum of all the forces exerted by all point charges present in the charge distribution.

Consider a charge distribution having n point charges, $q_1, q_2, q_3, \dots, q_n$ and position vectors $\vec{r}_1, \vec{r}_2, \vec{r}_3, \dots, \vec{r}_n$ respectively.

The force exerted by q_1 on any given charge q_0 having PV \vec{r}_0 is given as



$$\vec{F}_{01} = \frac{1}{4\pi\epsilon_0} \frac{q_1 q_0}{|\vec{r}_{10}|^2} \hat{r}_{10}$$

$$\Rightarrow \vec{F}_{01} = \frac{1}{4\pi\epsilon_0} \frac{q_1 q_0}{|\vec{r}_{10}|^3} \vec{r}_{10} \quad \left\{ \because \hat{A} = \frac{\vec{A}}{|\vec{A}|} \right\}$$

$$\Rightarrow \vec{F}_{01} = \frac{1}{4\pi\epsilon_0} \frac{q_1 q_0}{|\vec{r}_0 - \vec{r}_1|^3} (\vec{r}_0 - \vec{r}_1) \quad \left\{ \because \Delta \text{ law of vector addition} \right\}$$

$$\Rightarrow \text{Similarly } \vec{F}_{02} = \frac{1}{4\pi\epsilon_0} \frac{q_2 q_0}{|\vec{r}_0 - \vec{r}_2|^3} (\vec{r}_0 - \vec{r}_2)$$

$$\text{Similarly } \vec{F}_{0n} = \frac{1}{4\pi\epsilon_0} \frac{q_n q_0}{|\vec{r}_0 - \vec{r}_n|^3} (\vec{r}_0 - \vec{r}_n)$$

This from superposition principle net
classmate

force acting on the test charge q_0 due charge distribution is

$$\vec{F} = \vec{F}_{01} + \vec{F}_{02} + \dots + \vec{F}_{0n}$$

$$\Rightarrow \vec{F} = \frac{q_0}{4\pi\epsilon_0} \left[\frac{q_1}{|\vec{r}_0 - \vec{r}_1|^3} (\vec{r}_0 - \vec{r}_1) + \frac{q_2}{|\vec{r}_0 - \vec{r}_2|^3} (\vec{r}_0 - \vec{r}_2) + \dots + \frac{q_n}{|\vec{r}_0 - \vec{r}_n|^3} (\vec{r}_0 - \vec{r}_n) \right]$$

$$\Rightarrow \vec{F} = \frac{q_0}{4\pi\epsilon_0} \sum_{i=1}^n \frac{q_i}{|\vec{r}_0 - \vec{r}_i|^3} (\vec{r}_0 - \vec{r}_i)$$

Force on a given charge due continuous charge distribution

(a) Due to continuous line distribution of charge \rightarrow

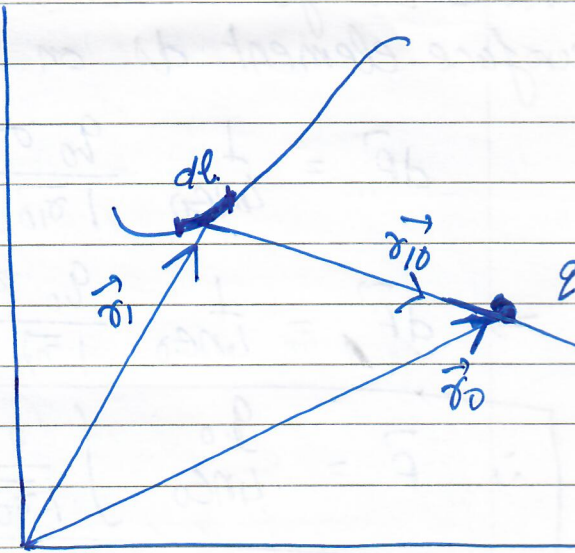
Consider a continuous line distribution of charge having linear charge density λ (charge per unit length)

Consider a small length element dl having charge λdl and having PV \vec{r}_i as shown.

Thus force exerted by small length element dl on a given charge q_0 having PV \vec{r}_0 is given as.

$$d\vec{F} = \frac{1}{4\pi\epsilon_0} \frac{q_0 \lambda dl}{|\vec{r}_{i0}|^2} \hat{r}_{i0}$$

$$\text{classmate} \Rightarrow d\vec{F} = \frac{1}{4\pi\epsilon_0} \frac{q_0 \lambda dl}{|\vec{r}_0 - \vec{r}_i|^3} (\vec{r}_0 - \vec{r}_i)$$



Thus force due to entire line distribution of charge

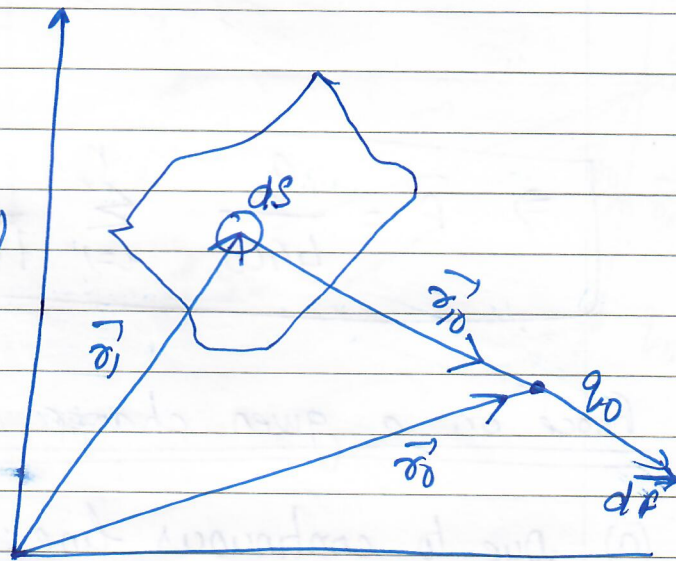
$$\text{Thus } \vec{F} = \int d\vec{F}$$

$$\Rightarrow \vec{F} = \frac{q_0}{4\pi\epsilon_0} \int \frac{d\lambda dl}{|\vec{r}_0 - \vec{r}_1|^3} (\vec{r}_0 - \vec{r}_1)$$

(b) Due to continuous surface distribution of charges

Consider a continuous surface distribution of charge having surface charge density σ (charge per unit surface area)

Consider a small surface element ds having charge σds and $PV \vec{r}_1$ as shown.



Small force exerted by surface element ds on a given charge q_0 having $PV \vec{r}_0$

$$d\vec{F} = \frac{1}{4\pi\epsilon_0} \frac{q_0 \sigma ds}{|\vec{r}_0|^2} \hat{r}_{10}$$

$$\Rightarrow d\vec{F} = \frac{1}{4\pi\epsilon_0} \frac{q_0 \sigma ds}{|\vec{r}_0 - \vec{r}_1|^3} (\vec{r}_0 - \vec{r}_1)$$

$$\therefore \vec{F} = \frac{q_0}{4\pi\epsilon_0} \int \frac{\sigma ds}{|\vec{r}_0 - \vec{r}_1|^3} (\vec{r}_0 - \vec{r}_1)$$

(c) Due to continuous volume distribution of charge:

Consider a continuous volume distribution of charge having volume charge density ρ (charge per unit volume)

consider a small volume element dV having charge ρdV and PV \vec{r}_1 as shown.

Thus small force exerted by by small volume element on a given charge q_0 having PV \vec{r}_0 is.

$$d\vec{F} = \frac{1}{4\pi\epsilon_0} \frac{q_0 \rho dV}{|\vec{r}_{10}|^2} \hat{r}_{10}$$

$$\Rightarrow d\vec{F} = \frac{1}{4\pi\epsilon_0} \frac{q_0 \rho dV}{|\vec{r}_0 - \vec{r}_1|^3} (\vec{r}_0 - \vec{r}_1)$$

$$\therefore \vec{F} = \frac{q_0}{4\pi\epsilon_0} \int \frac{\rho dV}{|\vec{r}_0 - \vec{r}_1|^3} (\vec{r}_0 - \vec{r}_1)$$

