

DATE

DUAL NATURE OF MATTER AND RADIATION

Free electrons in metals \Rightarrow Loosely bound electrons of the outer shell of an atom are called free electrons. These free electrons can move freely inside the lattice of +ve ions. However they can leave the surface of the metal at their own. So external energy has to be provided to these free electrons to eject them out of the metal surface.

The minimum amount of energy required by an electron to just escape from the metal surface is called work function of the metal.

The work function of the metal is denoted by w_0 and measured in electron volt. (eV).

The work function depends upon the nature of metal. Work function for caesium (Cs) is lowest (2.14 eV) and for platinum (Pt) is highest (5.65 eV).

Electron Volt \Rightarrow Energy gained by an electron when it is accelerated by applying a pot. diff. of 1 Volt is called 1 eV.

$$\text{ie } 1\text{eV} = 1\text{e} \times 1\text{V} \quad (w \text{ or } E = qV)$$

$$\Rightarrow 1\text{eV} = 1.6 \times 10^{-19} \text{C} \times 1\text{V}$$

$$= 1.6 \times 10^{-19} \text{CV}$$

$$\Rightarrow \boxed{1\text{eV} = 1.6 \times 10^{-19} \text{J}}$$

Electron Emission \rightarrow The phenomenon of emission of electron from the metal surface by giving it an energy more than the work function of the metal is called **electron emission**.

Electron emission can be of four types \rightarrow

1. **Thermionic emission** \rightarrow The emission of electrons on heating is called thermionic emission. Emitted e^- s are called thermions or thermo-electrons.
2. **Field Emission** \rightarrow The emission of e^- s from the metal surface by applying strong electric field is called field emission.
3. **Photo-electric emission** \rightarrow The phenomenon of emission of electrons from the metal surface when light of suitable high frequency falls on it is called photo-electric emission. The emitted electrons are photo-electrons.
4. **Secondary emission** \rightarrow When a fast moving electrons hit the metal surface, it ~~imparts its energy~~ imparts its energy to the free electron of the metal and produces secondary emission. The emitted electron is called secondary electron.

Photo-Electric Effect \rightarrow The phenomenon of emission of free electrons from the metal surface, when light of suitable high frequency falls on it is called photo electric effect.

The photo electric effect can be explained by considering the particle nature of light.

These particles of light are called photons.

Some basic properties of the photons are as under:-

1. Velocity of photon through free space is equal to velocity of light.
2. The speed of photon changes as it travels through different mediums-
3. The frequency of photon does not change as it travels through different mediums.
4. ~~and~~ As $\lambda = \frac{c}{\nu}$, Thus wave length also change through different mediums.
5. Energy of the photon;

$$E = h\nu$$

where $h = 6.63 \times 10^{-34} \text{ J s} = \text{Planck's const.}$

6. Mass of the photon moving with velocity u of light

$$m = \frac{m_0}{\sqrt{1 - \frac{u^2}{c^2}}}$$

Thus rest mass,

$$m_0 = m \sqrt{1 - \frac{u^2}{c^2}}$$

Since velocity of photon $u = \text{velocity of light } c$

$$\therefore m_0 = 0$$

7. The moving mass of the photon can be determined by using Einstein's mass energy relationship.

$$\text{i.e. } E = mc^2 = h\nu$$

$$\therefore m = \frac{h\nu}{c^2}$$

8. Thus momentum of the photon

$$\text{classmate } p = mc = \frac{h\nu}{c} = \frac{h}{\lambda}$$

9. Photons are electrically neutral. Hence can't be deflected by electric and magnetic field.
10. A photon may collide with material particle. In such collisions, total momentum and total energy remains conserved. However no. of photons may increase or decrease.
11. If intensity of light of given frequency is increased, then no. of photons increases however energy of each photons remains same.

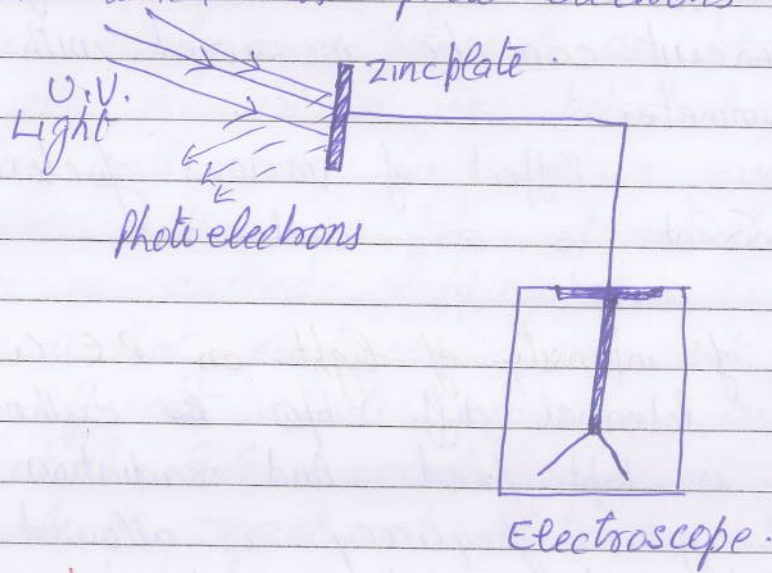
Experimental Study of photo-electric effect \rightarrow

Hertz's Observations \rightarrow While demonstrating the existence of electromagnetic waves, Hertz found that the sparks across the metallic spheres of detector can be obtained more easily, when the cathode was illuminated by the ultraviolet radiations. This happened because ultraviolet radiations caused the emission of electrons which enhanced the high voltage sparks.

Hallwachs's ~~and Lenard's~~ observations \rightarrow Hallwachs connected a zinc plate to an electroscope. He allowed ultraviolet light to fall on zinc plate and observed that

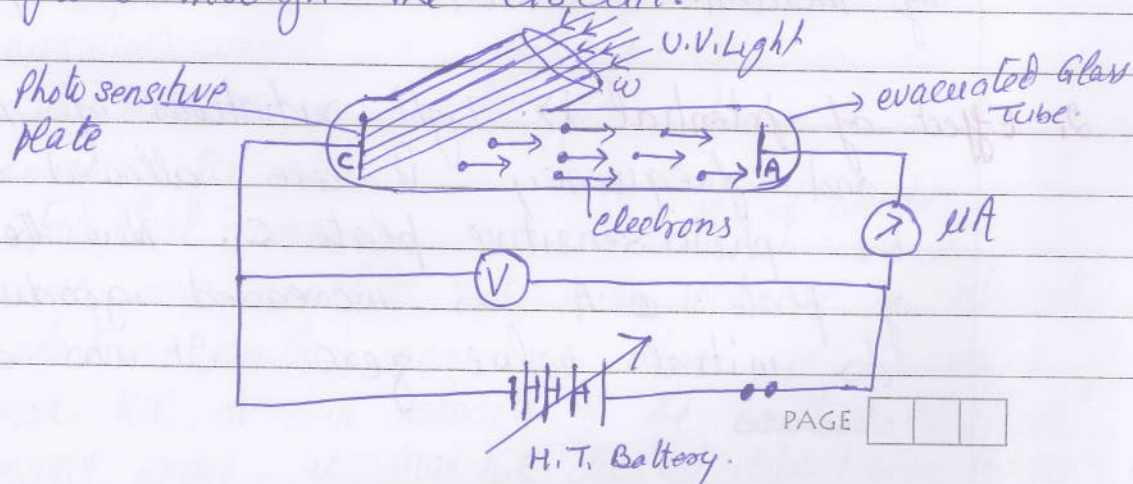
1. Zinc plate get uncharged if initially -vely charged
2. " " " +vely charged if " uncharged.
3. " " " more +vely charged if " +vely charged.

ie some ~~very~~ charged particles are being removed from the zinc plate when exposed to U.V. Light. Later on these particles are discovered to be electrons and named as photo electrons



Lenard's observations \rightarrow

Lenard observed that when U.V. radiations are allowed to fall on the emitter plate of an evacuated glass tube as shown, then current flows in the circuit. The current through the circuit stops as soon as the U.V. radiations are stopped. Lenard explained that as soon as the U.V. radiations fall on the emitter (Cathode) C, photoelectrons ~~are~~ emit from it and these electrons are attracted by the ~~very~~ char. +ve collector (Anode). Thus current k/a photoelectric current flows through the circuit.



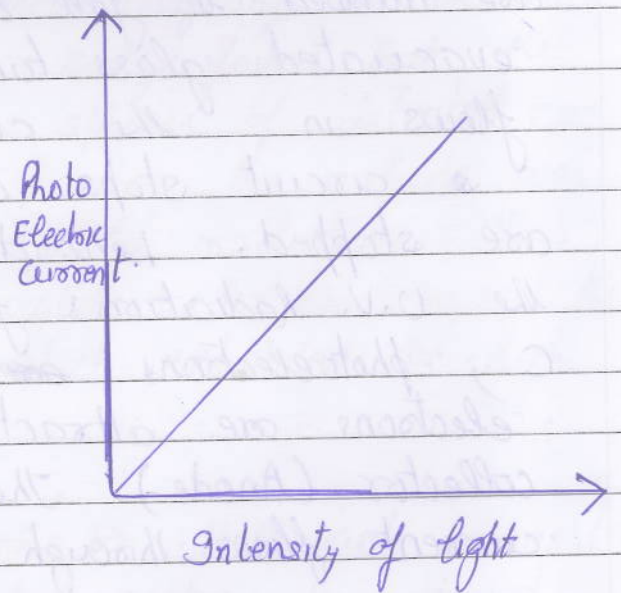
Potential applied across cathode C and anode A can be varied with the help of potential divider arrangement and its value can be noted from voltmeter. Where as current flowing through the circuit can be measured with the help of micro ammeter.

Effect of various factors on photo electric current is as under:-

① **Effect of intensity of light on P.E. Current** \rightarrow

Potential diff. b/w cathode C and anode A is kept fixed. And radiation of different intensities of given frequency is allowed to fall on the photosensitive plate C and the value of P.E. current flowing through circuit is measured with the help of micro ammeter.

It was observed that P.E. current varies linearly with intensity as shown in the graph. Thus it implies that number of photo electrons emitted per second is proportional to the intensity of incident radiation.



② **Effect of potential** \rightarrow Light radiations of intensity I_1 and frequency ν are allowed to fall on the photo sensitive plate C. Now the potential of plate A is increased gradually from its initial value zero. It was observed that

P.E. C increases with increase in +ve pot. of plate A and soon it attains saturated value. At this stage all the photoelectrons emitted by plate C are collected by anode A.

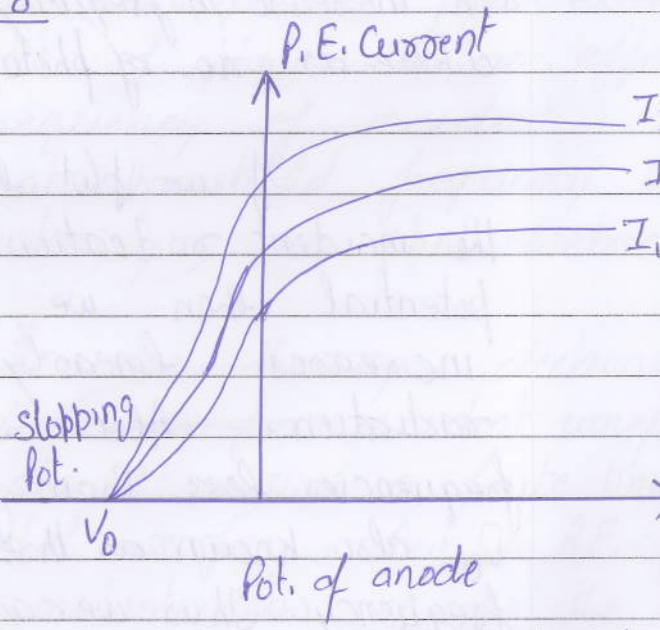
If we apply -ve potential on plate A, it is observed that with increase in -ve potential, P.E. current reduces sharply and soon for certain -ve pot. V_0 P.E. current becomes zero. This -ve pot. at which P.E. current becomes zero is called stopping potential or cut-off potential.

We know that electrons coming out from cathode C move with different velocities towards anode A. So at stopping potential, P.E. current is zero, i.e. no electron is able to reach at plate A. Thus we can say that potential energy due applied pot. V_0 has balanced the ~~max~~ max. Kinetic energy of the electron i.e.

$$eV_0 = \frac{1}{2} m v_{max}^2$$

$$\text{or } v_{max} = \sqrt{\frac{2eV_0}{m}}$$

If we repeat the experiment with different intensities I_2 and I_3 so that $I_3 > I_2 > I_1$, then we observe that the value of saturation current increases with increase in intensity, however the value of stopping potential remains same.

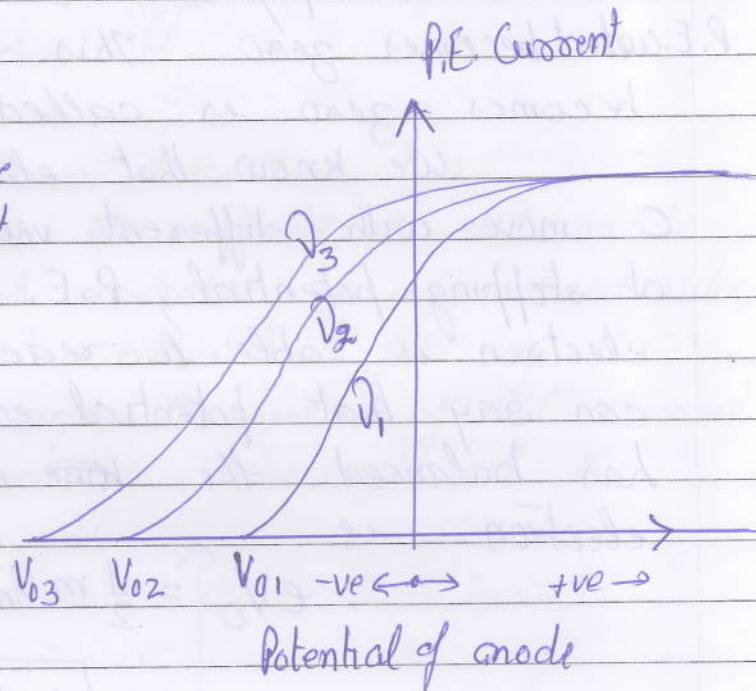


Thus we can conclude that with increase in intensity no. of photoelectrons emitted increases whereas the value of classmate max. K.E or max velocity of the emitted electrons remains same. i.e. max K.E does not depend upon intensity of radiation.

③ Effect of freq. of incident radiation on stopping pot.

If we repeat the above experiment for three different radiations of same intensity but of different frequencies ν_1, ν_2, ν_3 so that $\nu_3 > \nu_2 > \nu_1$, then the graphs obtained are as shown.

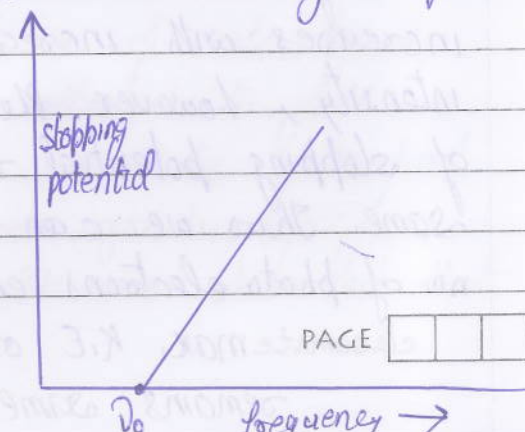
From the graphs it is clear that stopping pot increases with increase in frequency of incident radiation. However the value of saturation current remains same.



Thus we can say that max K.E or max velocity of the emitted photo electrons increases with increase in frequency

where as no. of photo electrons emitted remains same.

If we plot the graph b/w frequency of the incident radiation and corresponding stopping potential then we find that stopping potential increases linearly with frequency of incident radiation. Also stopping potential is zero for frequencies less than frequency ν_0 also known as threshold frequency. Thus we can say no photo electric emission takes place for a frequency less than
classmate threshold frequency.
 (what so ever be the value of intensity.)



Laws of photoelectric effect \rightarrow

- ① The P.E. emission is an instantaneous process.
- ② Photoelectric current is directly proportional to the intensity of incident radiation.
- ③ The K.E of the emitted photoelectrons is independent of the intensity of incident radiations and depends only upon the frequency of incident radiations.
- ④ The photoelectric emission takes place only above certain frequency of incident radiation k/a threshold freq.

Failure of classical wave theory \rightarrow

Ques \rightarrow Explain why photoelectric effect cannot be explained on the basis of wave nature of light.

Ans \rightarrow According to wave theory of light, with increase in intensity of incident light wave, the energy density of the wave also increases. Hence waves of higher intensity should be able to escape the photoelectrons. But the experimental studies of photo-electric effect suggests that if the frequency of incident radiation is less than threshold frequency then what so ever be its intensity, no photoelectric emission will take place.

Further according to wave theory, electrons will absorb energy from the ~~wave~~ incident wavefront slowly and slowly so it should require a finite time to escape from the metal surface. But in P.E. effect emission of electrons is instantaneous i.e. as the light falls on the ~~sa~~ metal surface, photoelectric emission takes place.

classmate Thus on the basis of above two facts we can say that a wave theory fails to explain P.E. effect.

Einstein's theory of Photo-Electric effect \rightarrow

Einstein explained photo electric effect on the basis of Plank's quantum theory.

The main features of Einstein's theory of P.E. effect are.

① Photoelectric emission is the result of interaction b/w the photon of incident radiation and electron of photosensitive plate. More importantly each photon can eject only one photo-electron.

② Each photon on collision with electron, imparts its entire energy to the electron and electron uses consumes this energy in two parts i.e.

(a) ~~while~~ Energy equals to the work function (w_0) of the metal is used while coming to the metal surface and.

(b) Remaining energy of the photon is used in gaining the kinetic energy.

③. ~~Very~~ $h\nu = w_0 + \frac{1}{2} m v_{\max}^2$ ——— ①

if the incident photon is threshold frequency ν_0 then electron will just escape from the metal surface and its K.E will be zero.

\therefore if $\nu = \nu_0$

then $\frac{1}{2} m v_{\max}^2 = 0$

Thus eqn. no. ① becomes

$$h\nu_0 = \omega_0 + 0$$

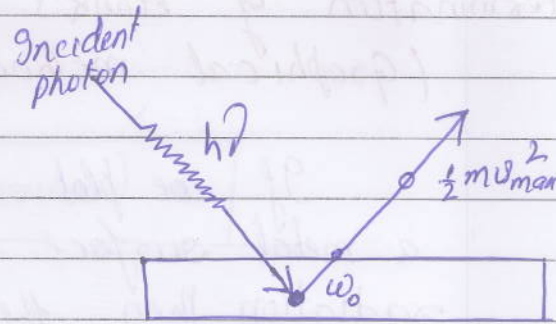
$$\Rightarrow \omega_0 = h\nu_0$$

Substitute ω_0 in eqn no ①
we get

$$h\nu = h\nu_0 + \frac{1}{2}mv_{max}^2$$

$$\Rightarrow \frac{1}{2}mv_{max}^2 = h\nu - h\nu_0$$

$$\Rightarrow \boxed{\frac{1}{2}mv_{max}^2 = h(\nu - \nu_0)} \longrightarrow \text{Einstein's eqn of photo electric effect.}$$



Explanation of laws of photo electric effect on the basis of Einstein's theory of P.E. effect / emission \rightarrow .

① Incident photon imparts its entire energy ($h\nu$) in go. i.e. energy is not absorbed by the electron from the incident wavefront slowly and slowly. Thus photo electric emission takes place instantaneously.

(2) Since according to Einstein's theory, each photon can eject only one electron. Thus no. of photo electrons emitted and hence the photo electric current depends upon the no. of incident photons i.e. intensity of incident radiation.

3. According to Einstein's eqn. of photo electric effect, K.E. of the emitted photo electron ($\frac{1}{2}mv_{max}^2$) depends upon the frequency (ν) of incident photon (radiation).

4. If $\nu < \nu_0$ then from Einstein's eqn. K.E. of the emitted electron will be $-ve$, which is not possible. Thus photo electric emission will take place only above threshold frequency.

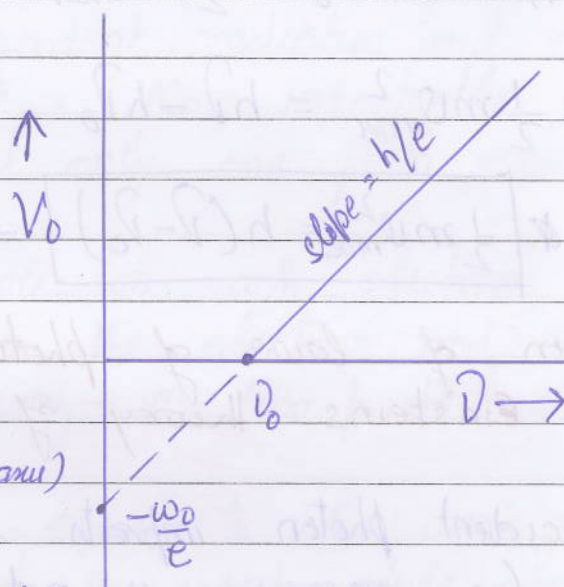
Determination of Plank's constant and work function \rightarrow (Graphical method)

If we plot the graph b/w stopping pot. for a metal surface with frequency of incident radiation then the graph obtained is a straight inclined line as shown.

From eqn of straight line,

$$y = mx + c \quad \text{--- (1)}$$

where m is slope of the line and c is y intercept (or intercept on vertical axis)



Also from Einsteins eqn of Photo electric effect.

$$K.E_{max} = h\nu - h\nu_0$$

$$\Rightarrow K.E_{max} = h\nu - w_0 \quad \text{--- (2)}$$

$$\text{also } K.E_{max} = eV_0 \quad \text{--- (3)}$$

from (2) and (3)

$$eV_0 = h\nu - w_0$$

$$\therefore V_0 = \frac{h}{e}\nu + \left(\frac{-w_0}{e}\right) \quad \text{--- (4)}$$

comparing eqn. no. (4) with eqn no (1) we get

$$m = \frac{h}{e}$$

$$\therefore h = m \times e$$

$$\Rightarrow \boxed{h = (\text{slope of } V_0 - \omega \text{ curve}) e}$$

also $-\frac{\omega_0}{e} = c$

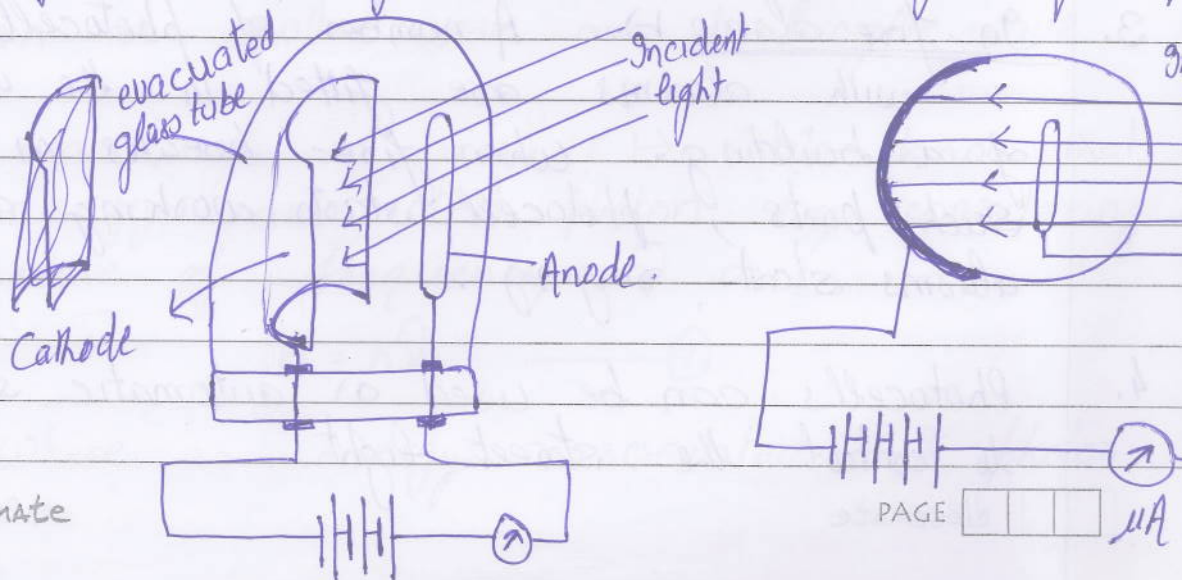
$$\Rightarrow -\frac{\omega_0}{e} = \gamma \text{ intercept}$$

$$\therefore \boxed{\omega_0 = e (\text{magnitude of intercept on vertical axis})}$$

The values of h and ω_0 determined graphically for sodium agreed well with the values known from other experiments.

Photo cell \rightarrow A photo cell or photo-electric cell is a device which converts light energy into electrical energy. It works on the principle of P.E. effect.

Construction and working \rightarrow It consists of a semi cylindrical cathode made up of a photo sensitive material and anode made up of thin wire in the form of loop.



When light of frequency greater than threshold frequencies falls on the cathode, photoelectrons are emitted by it and these emitted electrons are attracted by the anode and current starts flowing through the circuit. Since this photoelectric current is very feeble this is first amplified before using for useful purpose.

Applications of photocells \rightarrow

① A photocell connected to counter can be used as counting device, provided the persons enter one by one. As the person enters the room/hall it intercepts the light and photocell stops working, and counter counts the number of times photocell stops working.

2. In burglar alarms \rightarrow when a person enters in the prohibited area, it intercepts the invisible ultraviolet light falling on the photocell. This photocell is connected to alarm which starts ringing as photocell stops working.

3. In fire alarms \rightarrow A number of photocells attached with alarms are fitted in the various parts of a building. When fire breaks in one of such parts, photocell starts working and alarms start ringing.

4. Photocells can be used as automatic switches to control the street light.

5. To determine the opacity of solids and liquids.
6. In locating the minor flaws or holes in large metal sheets.
7. As a comparison meters.
8. In finding out the amount of day light (during bad light appears in matches).

Dual Nature of radiation and matter \rightarrow Some phenomena of light like diffraction, interference, polarization can only be explained by considering light as wave whereas some other phenomena like photoelectric effect, Compton effect etc can only be explained by considering light as particles. This shows that light has dual nature i.e. wave nature as well as particle nature.

In 1924, De Broglie argued that nature (universe) is made up of either mass or energy, and since nature loves symmetry therefore as the light radiations (energy) has dual nature hence material particles (mass) must also have dual nature.

He gave the theory that material particles in motion must possess wave and is known as matter wave or de-Broglie wave.

de-Broglie wave length of matter \rightarrow We know that energy associated photon by considering it as wave of frequency ν is,

$$E = h\nu \quad \text{--- (1)}$$

Where as energy associated with photon

by considering it as a particle of mass m

$$E = mc^2 \quad \text{--- (2)}$$

from (1) and (2),

$$h\nu = mc^2$$

$$\Rightarrow \frac{hc}{\lambda} = mc^2$$

$$\Rightarrow \lambda = \frac{hc}{mc^2}$$

$$\Rightarrow \boxed{\lambda = \frac{h}{mc}}$$

Whereas for some other particles like proton, neutron or electron of mass m and moving with velocity u , the de-Broglie wavelength of particle can be given as

$$\boxed{\lambda = \frac{h}{m u}}$$

$$\text{or } \boxed{\lambda = \frac{h}{p}}$$

This is also k/a de-Broglie's wave equation for material particle.

Note

if $u = 0$ then $\lambda = \infty$. That is no de-Broglie wave is associated with the particle which is at rest.

Also de-Broglie matter wave can't be considered as em wave. Because em wave are associated only with accelerated charged particles only.

whereas for de Broglie waves neither charge is required nor acceleration is required (only mo

de-Broglie wave length of an electron \rightarrow

Consider an electron of mass m is accelerated by applying a pot. diff of V volts. Let u is the velocity gained by the electron at rest then the K.E of the electron is as a result of work done on it by the applied potential

$$\frac{1}{2} m u^2 = eV$$

$$\Rightarrow \frac{p^2}{2m} = eV$$

$$\Rightarrow p = \sqrt{2meV}$$

$$\left\{ \begin{aligned} \therefore \text{K.E} &= \frac{1}{2} m u^2 \\ &= \frac{m^2 u^2}{2m} \\ &= \frac{p^2}{2m} \end{aligned} \right.$$

Thus wave length associated with the electron

$$\lambda = \frac{h}{p}$$

$$\Rightarrow \lambda = \frac{h}{\sqrt{2meV}}$$

on substituting the standard value of h , m , and e . we get,

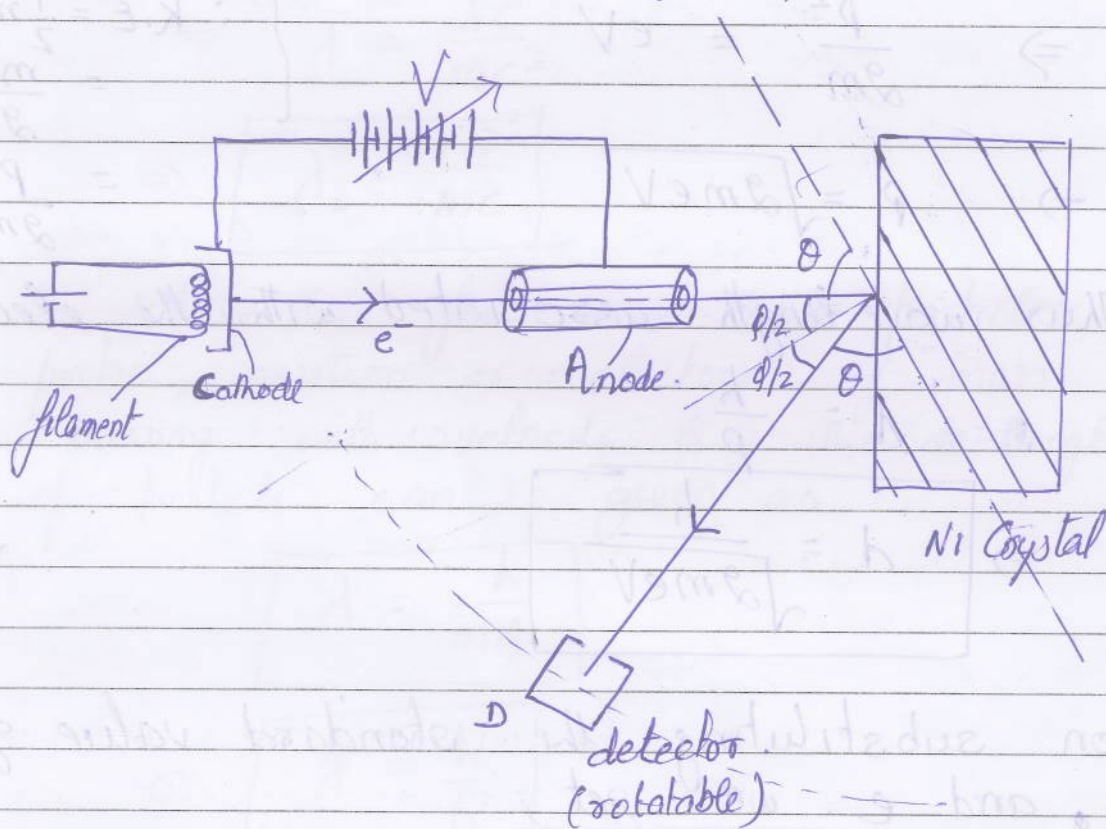
$$\lambda = \frac{12.27}{\sqrt{V}} \text{ \AA}$$

This value is of the same order as is obtained through experiments. de-Broglie was awarded the Nobel Prize in Physics in 1929 for this discovery.

Experimental demonstration of wave nature of electrons

oo Davison and Germer's experiment. \rightarrow

In Davison and Germer's experiment, electrons emitted from the hot cathode are accelerated by applying a suitable potential difference V . This fine beam of electrons is allowed to fall on a nickel crystal cut diagonally.



The electron beam scattered at various scattering angles were received by the rotatable detector D .

This experiment was repeated at various accelerating potential b/w $44V$ to $68V$ and it was observed that intensity of scattered beam of electron was maximum for the scattering angle of 50° and for an accelerating potential of $54V$.

It was explained that it happened so because

of formation of diffraction maxima of first order
the atoms of Ni crystal.

from the figure it is clear that

$$\theta + \phi + \theta = 180^\circ$$

where θ is glancing angle

$$\Rightarrow 2\theta = 180 - \phi$$

$$\Rightarrow \theta = \frac{180 - \phi}{2}$$

for first order diffraction maxima

$$\phi = 50^\circ$$

$$\therefore \theta = \frac{180 - 50}{2} = \frac{130}{2} = 65^\circ$$

Also from Bragg's law, for first order diffraction
maxima

$$2d \sin \theta = n\lambda$$

$$\text{or } \lambda = 2d \sin \theta$$

where $d = 0.91 \text{ \AA} =$ interatomic separation in Ni

and $\theta = 65^\circ =$ glancing angle.

on substituting the values.

$$\lambda = 2 \times 0.91 \times \sin 65^\circ$$

$$\Rightarrow \lambda = 1.65 \text{ \AA}$$

from de-Broglie's hypothesis at 54V pot.

$$\lambda = \frac{12.27}{\sqrt{54}} = 1.67 \text{ \AA}$$

This value is very close to the experimental value of Davison
and Germer. Thus we can say that Davison and Germer have
experimentally established the de-Broglie's hypothesis.